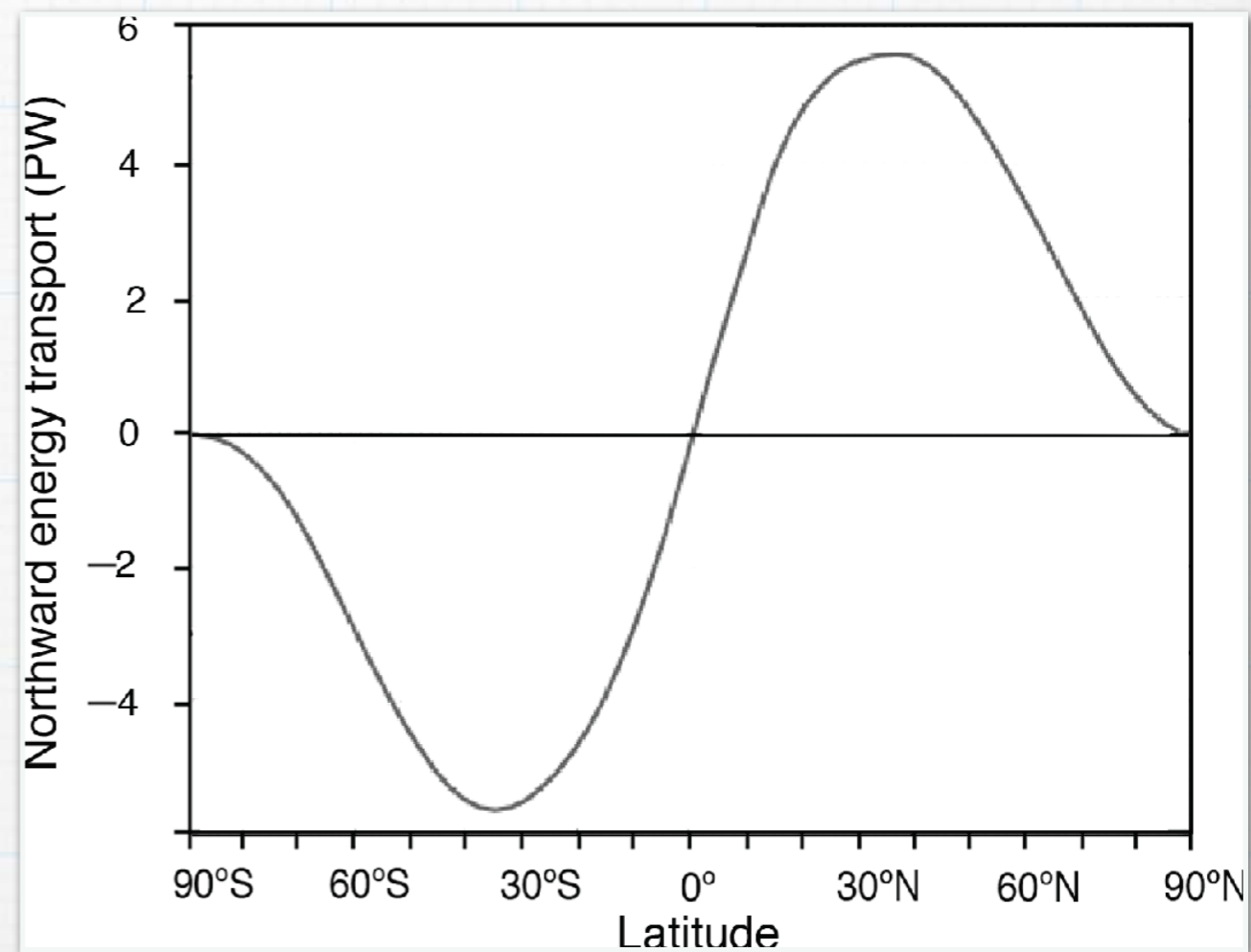
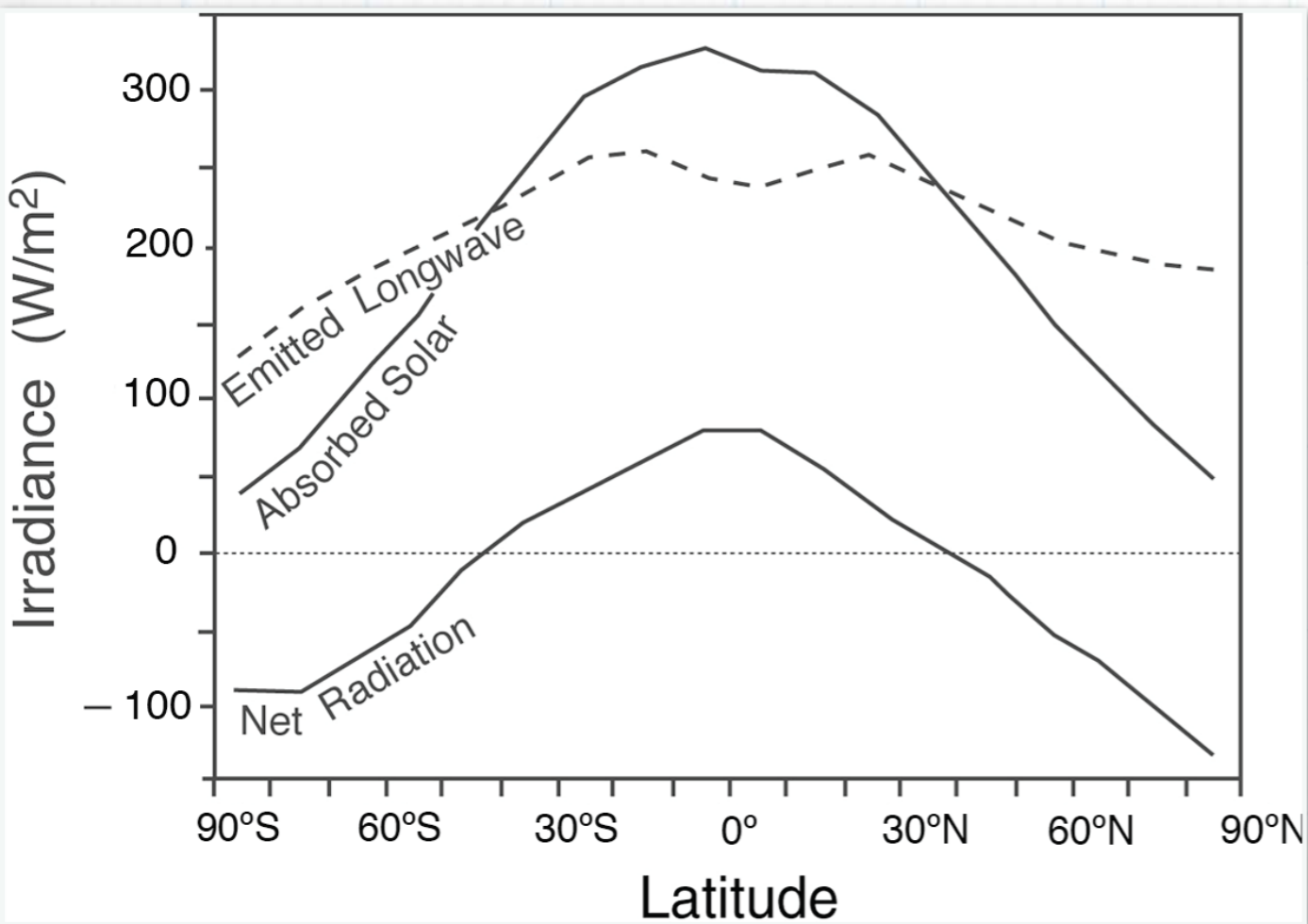


Atmosphere: #3

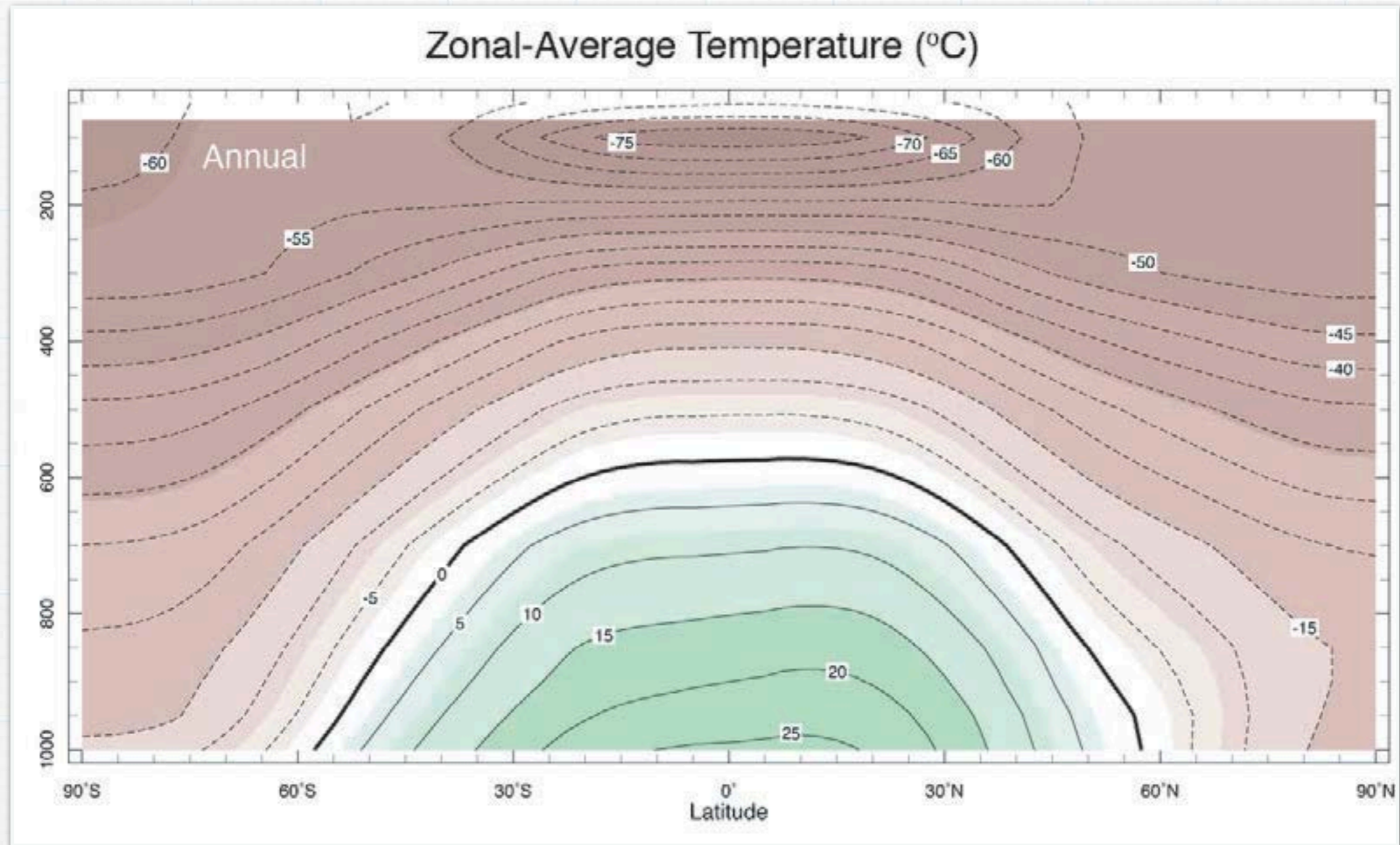
Observations

Radiative imbalance

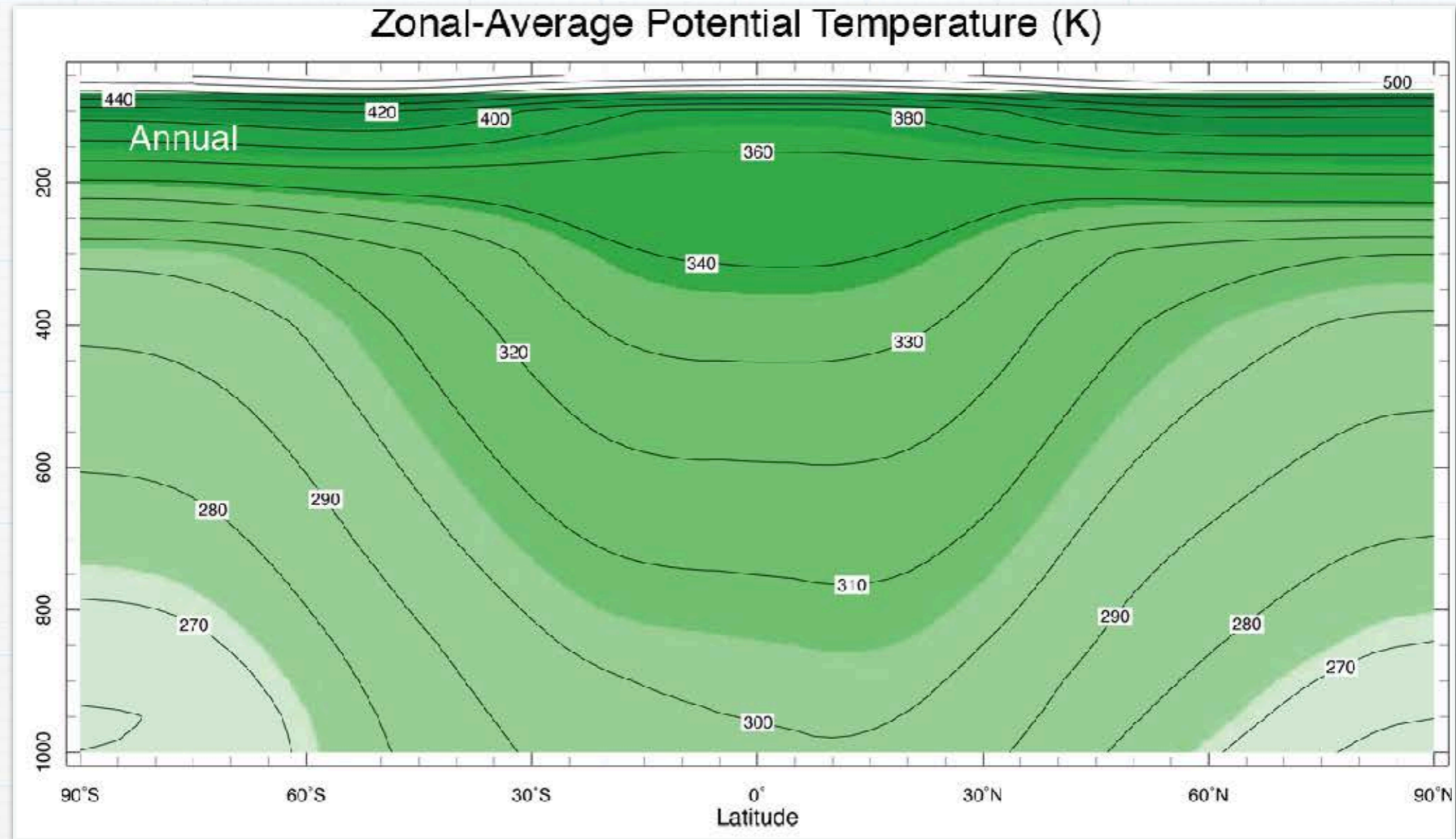


Temperature

- See how the radiative imbalance shapes T



Temperature: potential temperature



Pressure / geopotential height

- We are interested in $z(p)$, rather than $p(z)$
- From a hydrostatic balance and perfect gas law,

$$\frac{\partial z}{\partial p} = -\frac{RT}{gp}$$

$$z(p) = R \int_p^{p_s} \frac{T}{g} \frac{dp}{p}$$

- $z(p)$ is called **geopotential height**.

Pressure / geopotential height

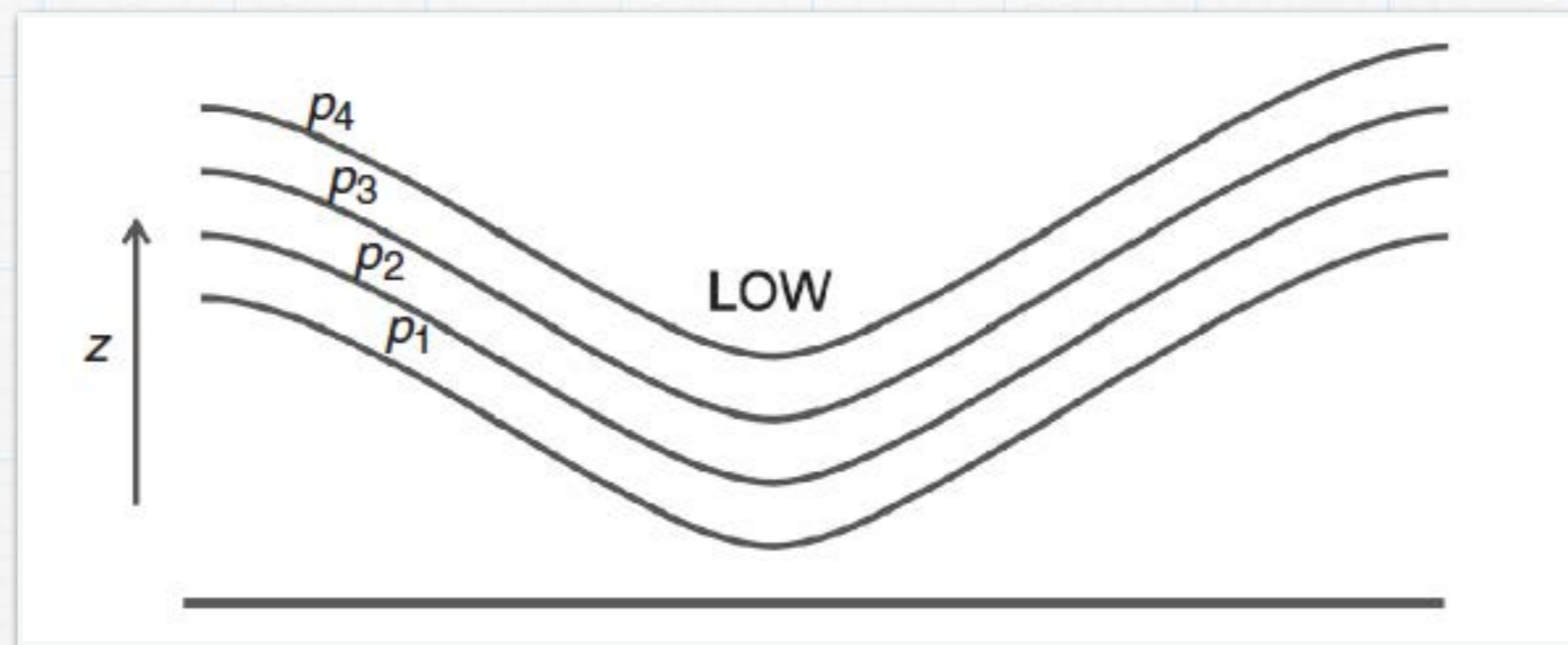
- If we assume that g and T do not vary a lot with p ,

$$z(p) = \frac{RT}{g} (\ln p_s - \ln p)$$

- z increases as p decreases.
- Higher T increases geopotential height.

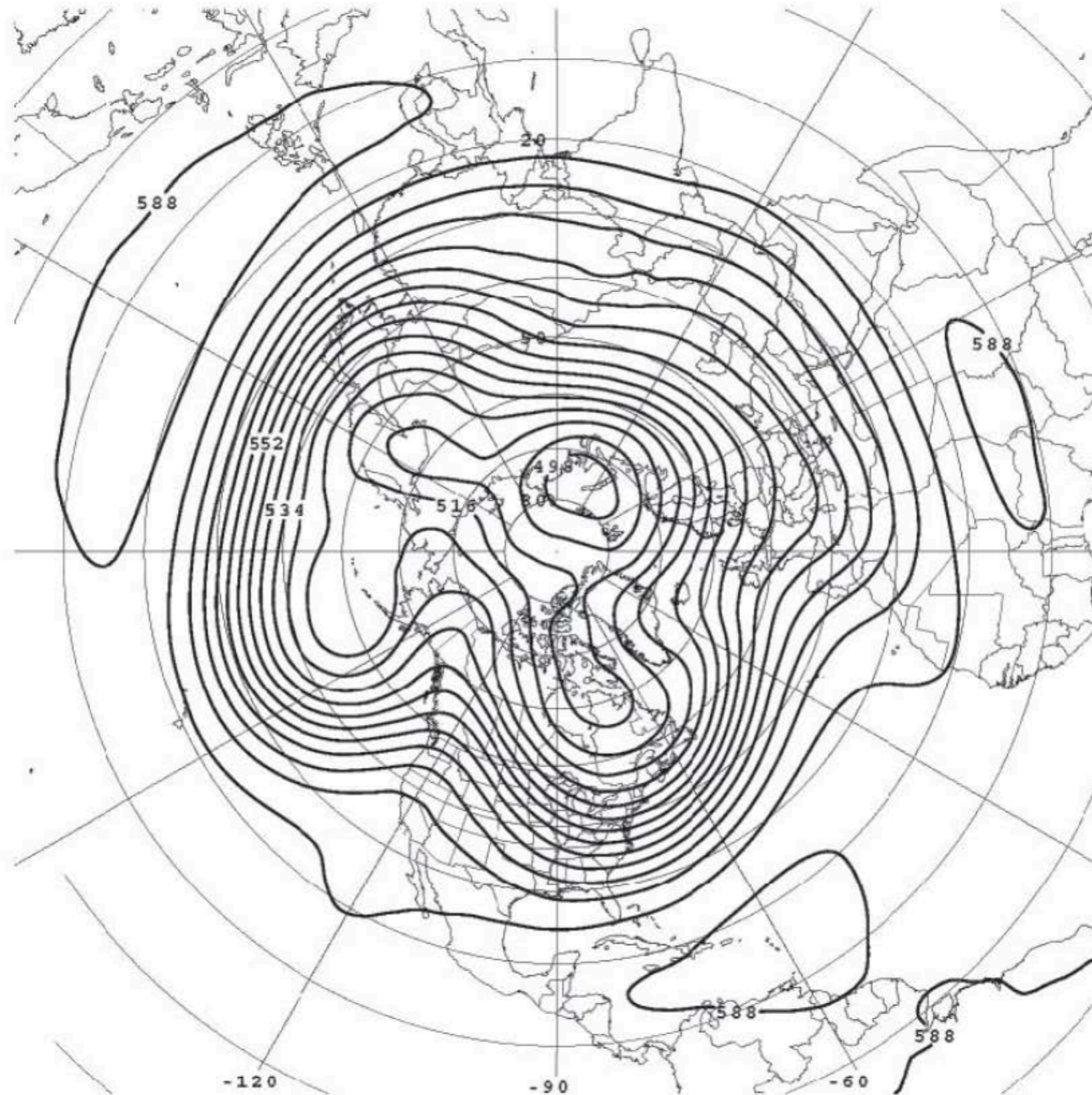
Pressure / geopotential height

- Geopotential height is lower at the low pressure system.
- Or the high pressure system corresponds to the high geopotential height.
- T tends to be low in the region of low geopotential height.



Pressure / geopotential height

The mean height of the 500 mbar surface in January , 2003



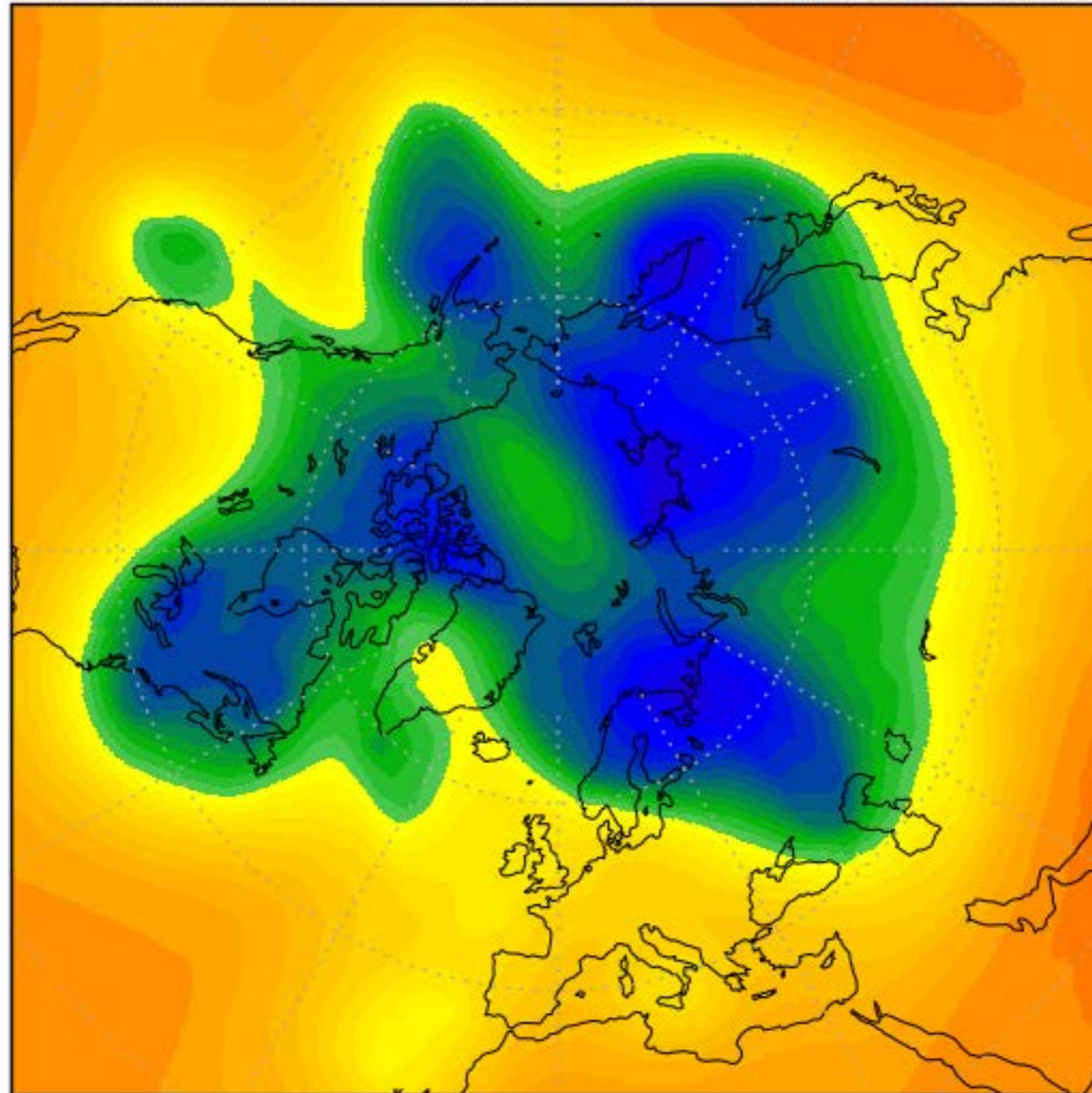
Pressure / geopotential height

CMC GPDS 0.15: 500 hPa geopotential height (dam)

Init: Mon 28 Mar 2022, 00Z

Fcst: +006H

Valid: Mon 28 Mar 2022, 06Z



486 494 502 510 518 526 534 542 550 558 566 574 582 590 598 606

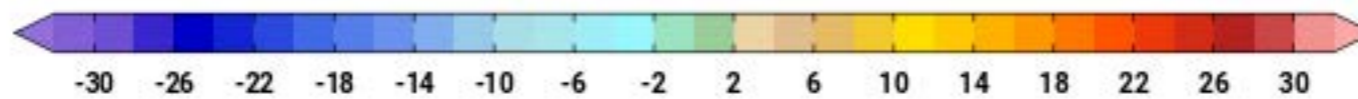
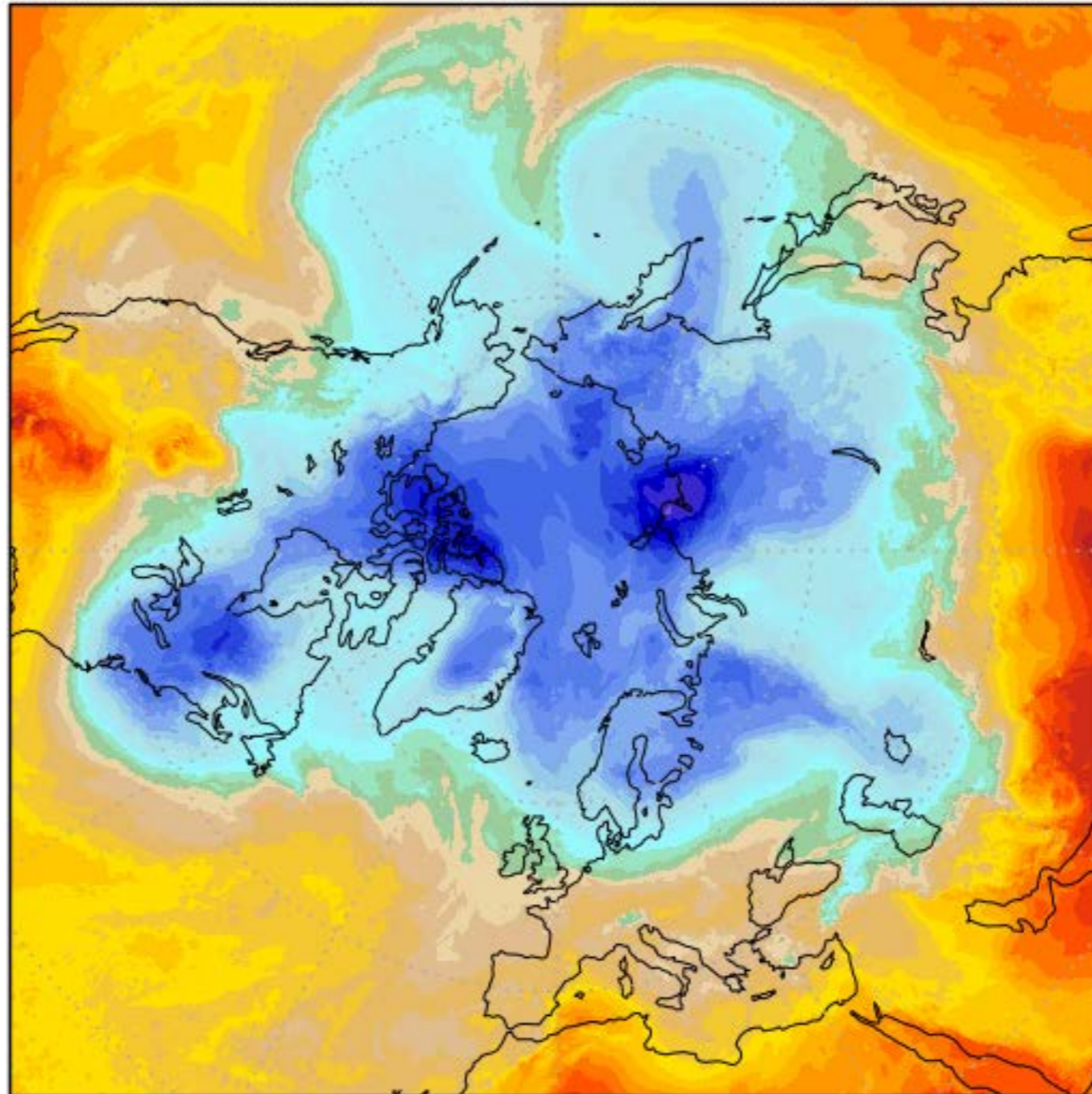
Pressure / geopotential height

CMC GPDS 0.15: 850 hPa temperature (C)

Init: Tue 29 Mar 2022, 00Z

Fcst: +006H

Valid: Tue 29 Mar 2022, 06Z



Pressure / geopotential height

- We can discuss about the slope of the geopotential height if we know the temperature.

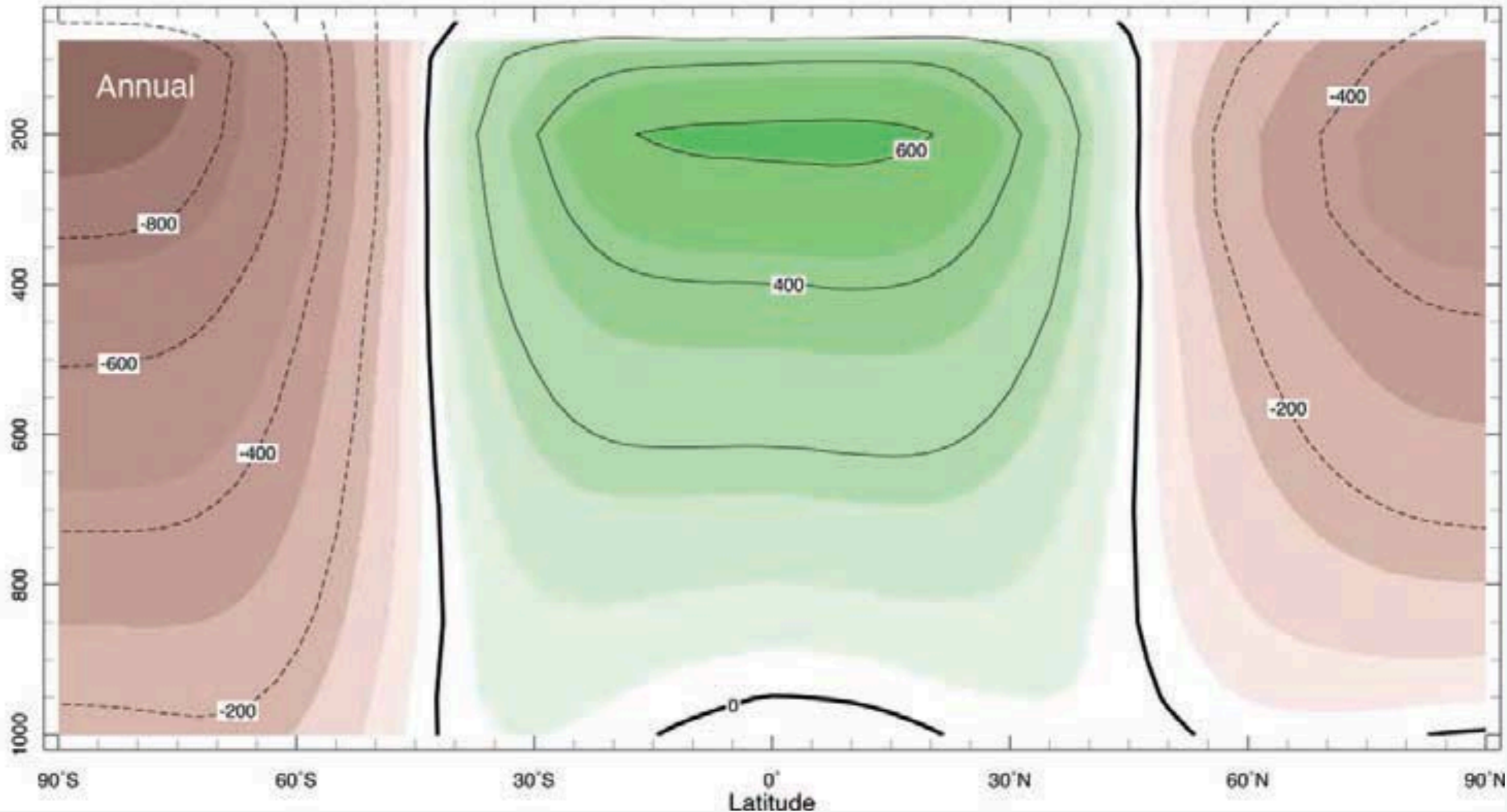
$$z_{warm} - z_{cold} = \frac{R}{g} (T_{warm} - T_{cold}) (\ln p_s - \ln p)$$

- We can also discuss about the thickness of an atmospheric layer if we know the temperature.

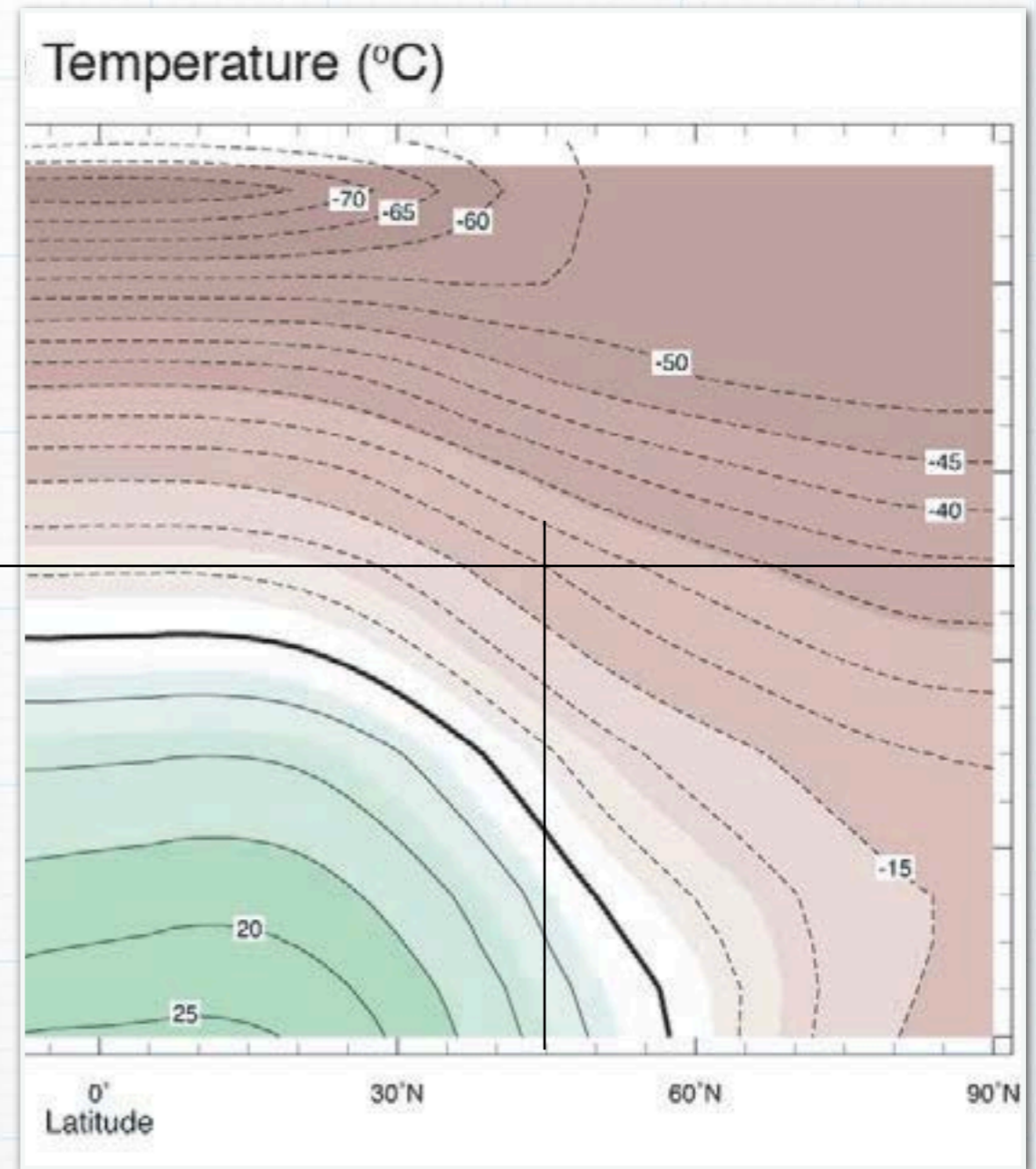
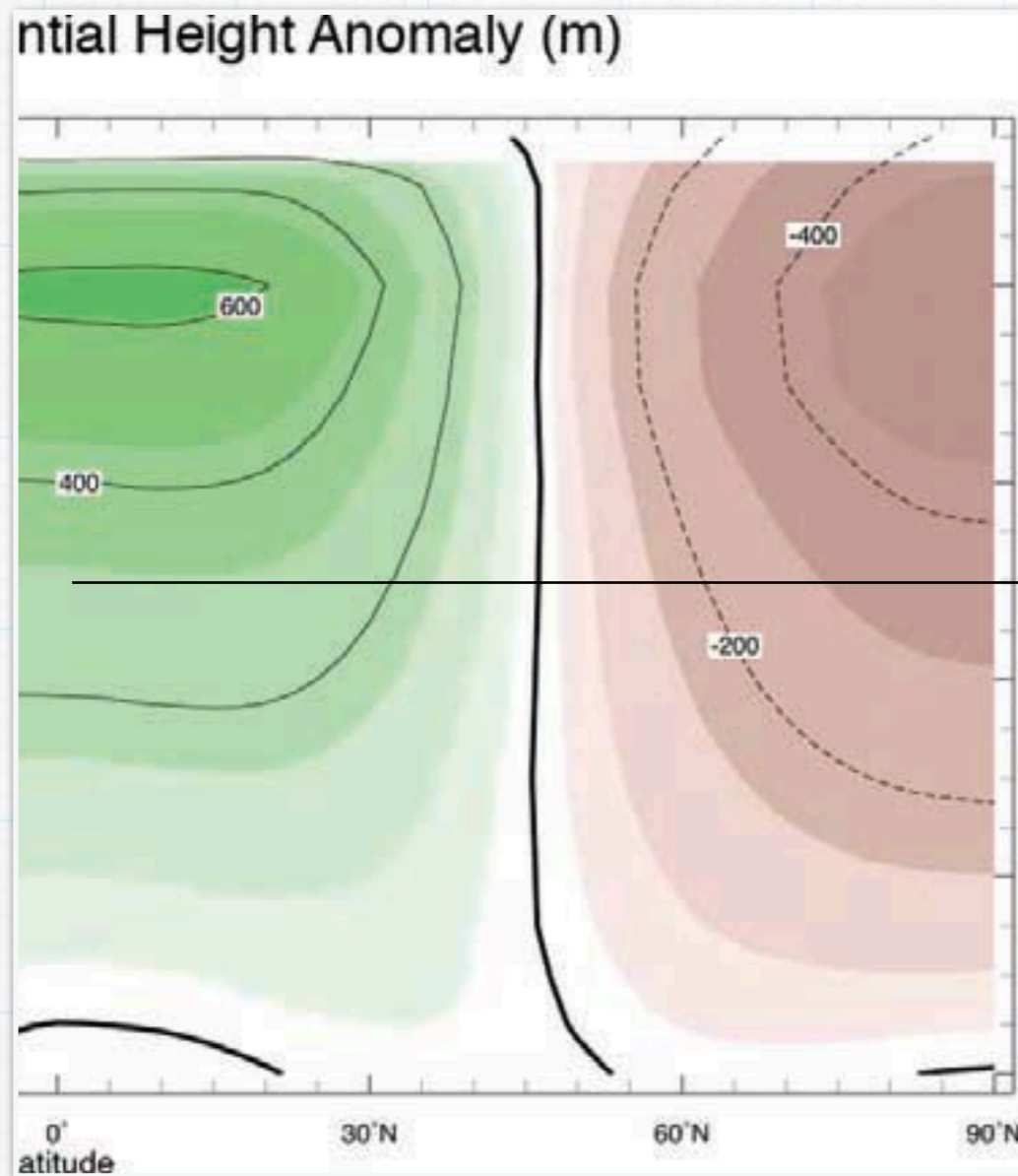
$$z_{p_1} - z_{p_2} = \frac{R\bar{T}}{g} (\ln p_2 - \ln p_1)$$

Pressure / geopotential height

Zonal-Average Geopotential Height Anomaly (m)

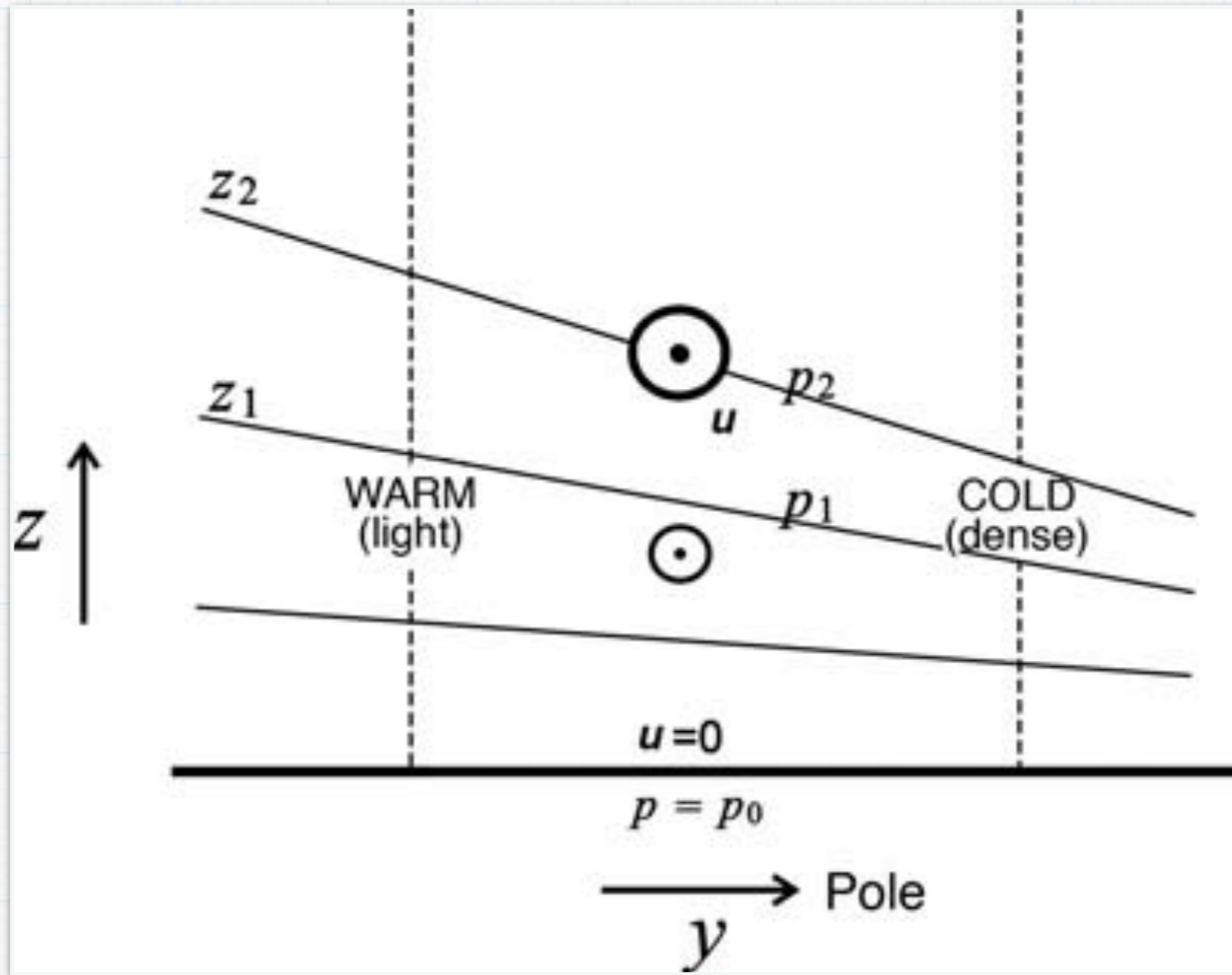


Pressure / geopotential height

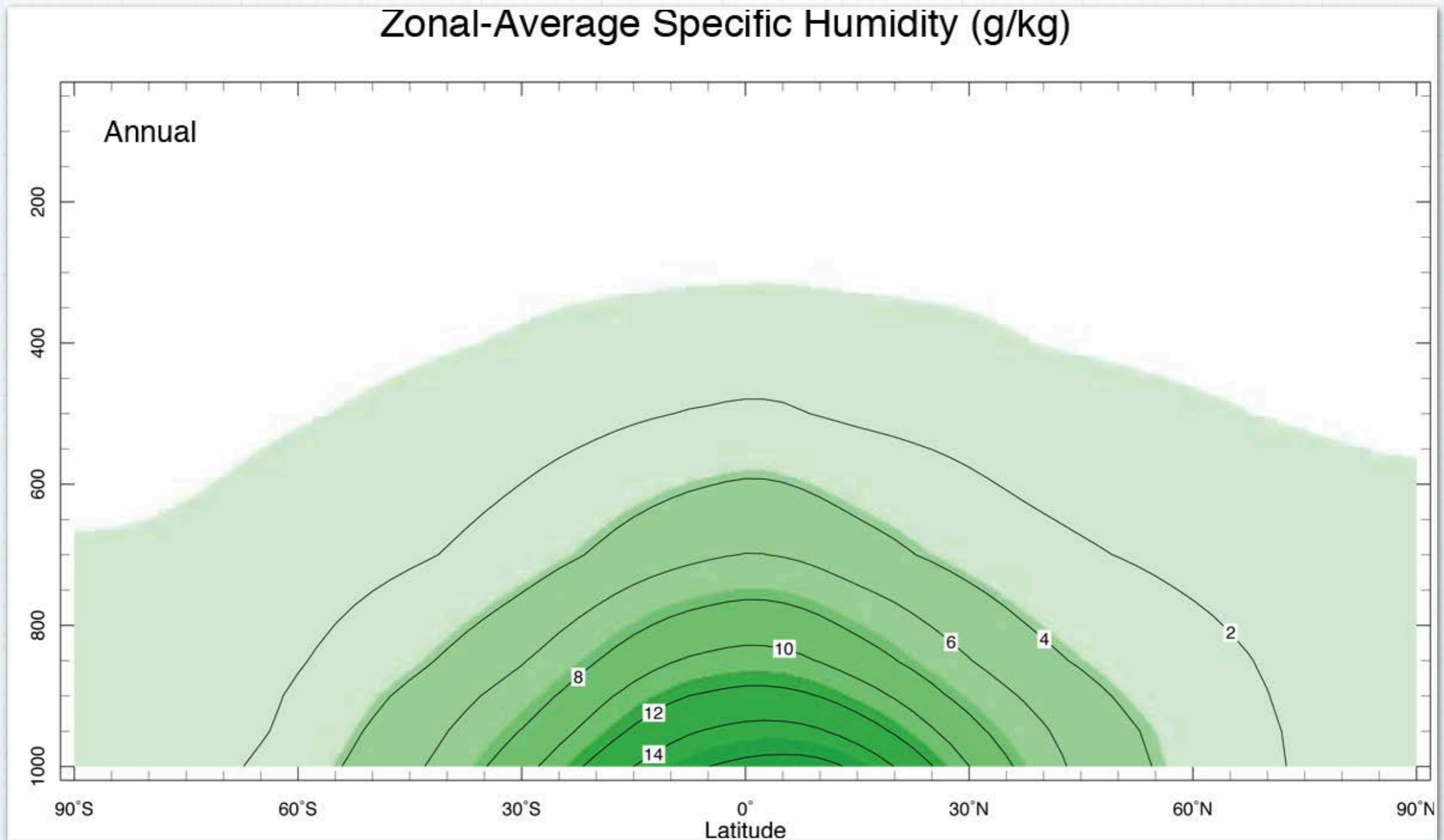


$$z_{warm} - z_{cold} = \frac{R}{g} (T_{warm} - T_{cold}) (\ln p_s - \ln p)$$
$$\approx \frac{287 \times 20}{10} \ln \left(\frac{1000}{500} \right) \approx 400$$

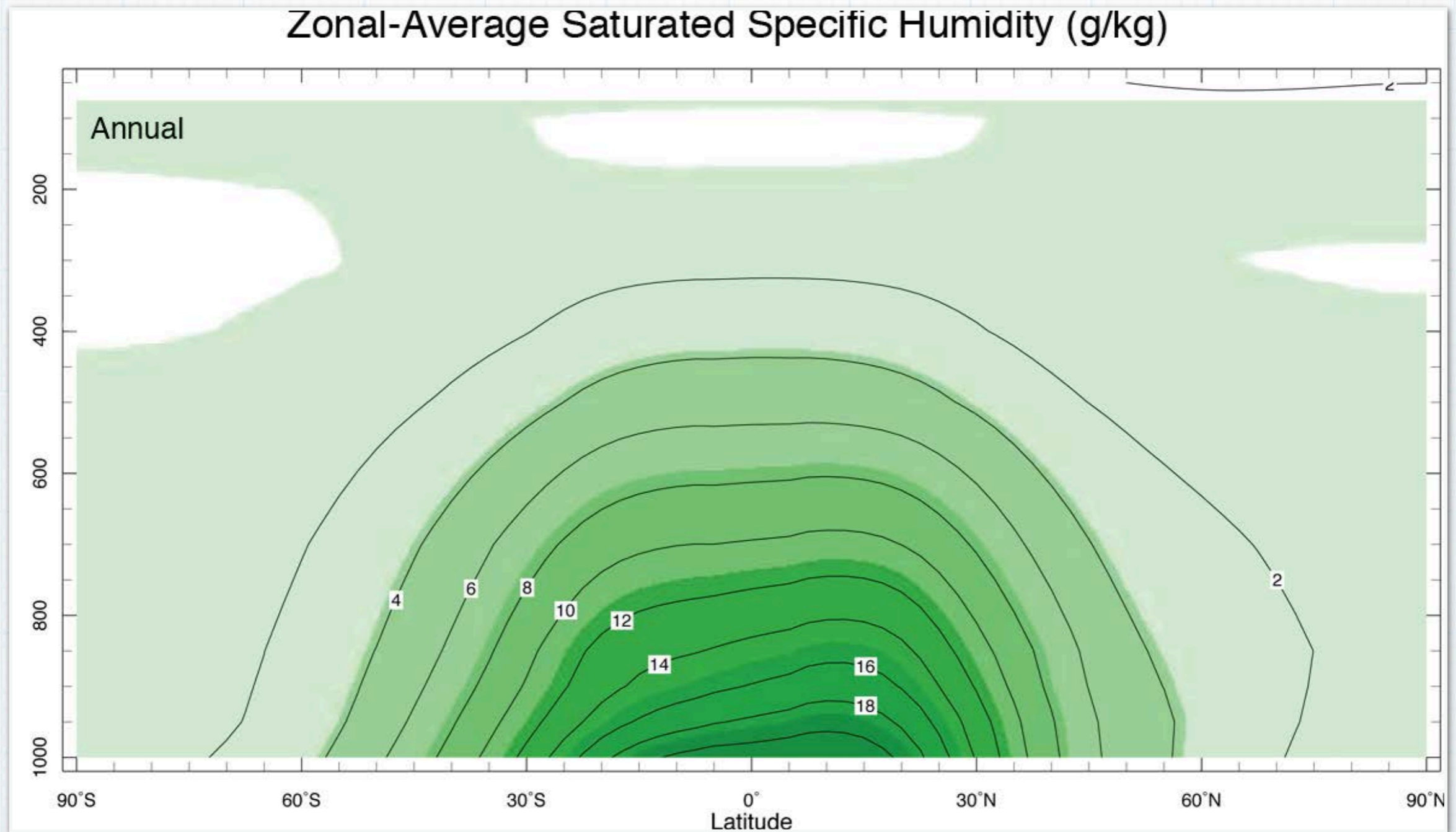
Pressure / geopotential height



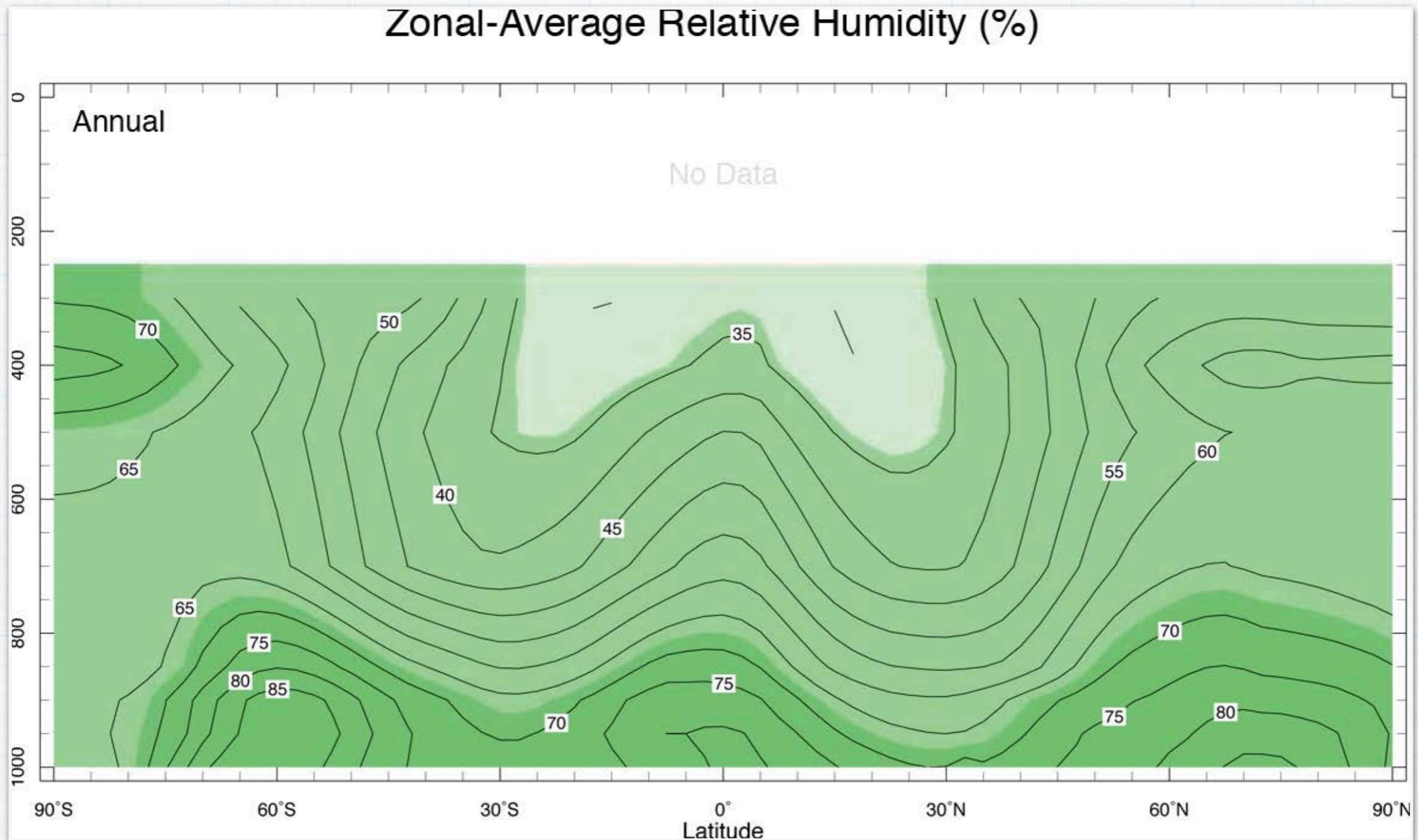
Humidity: specific humidity



Humidity: saturated specific humidity



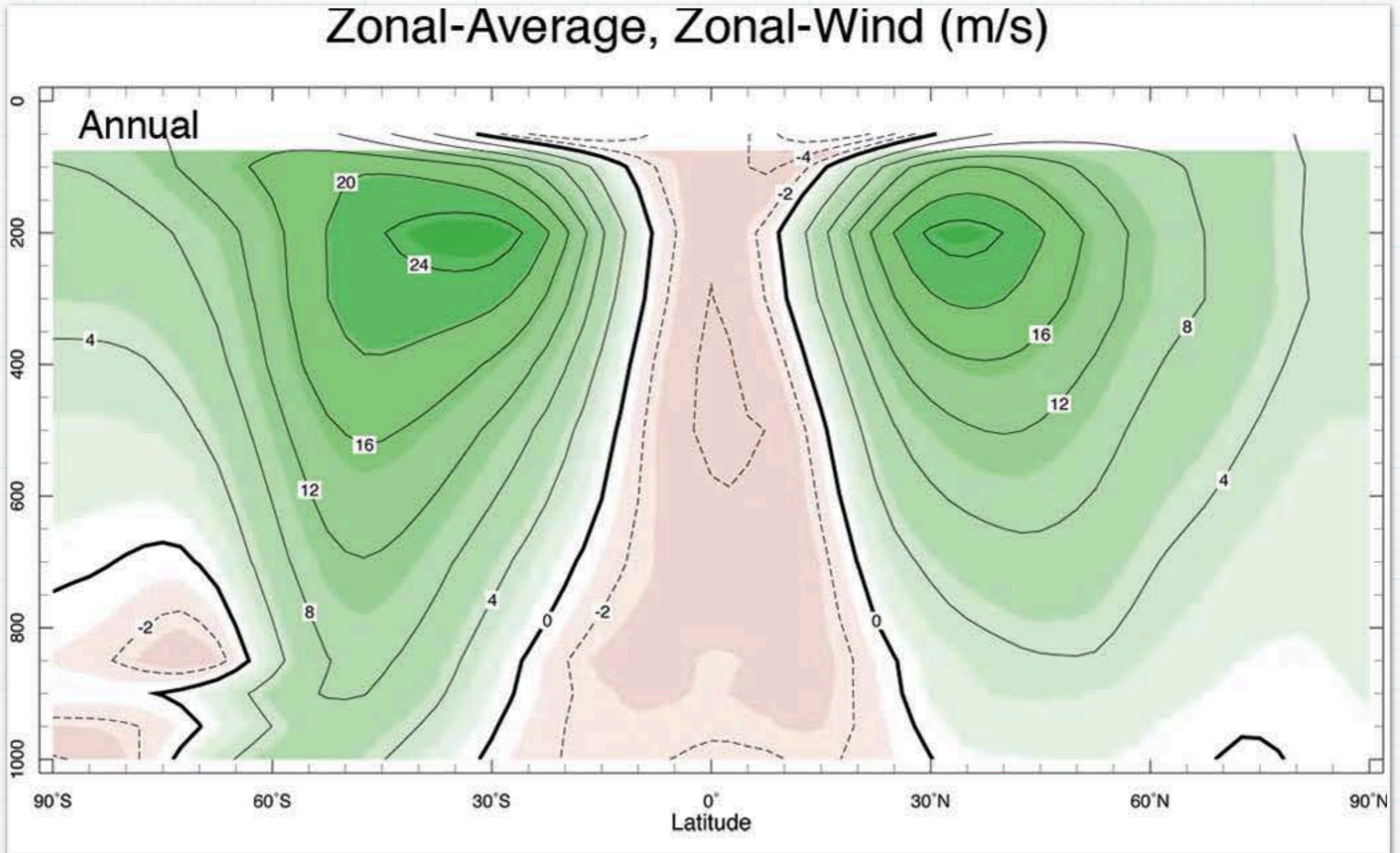
Humidity: saturated specific humidity



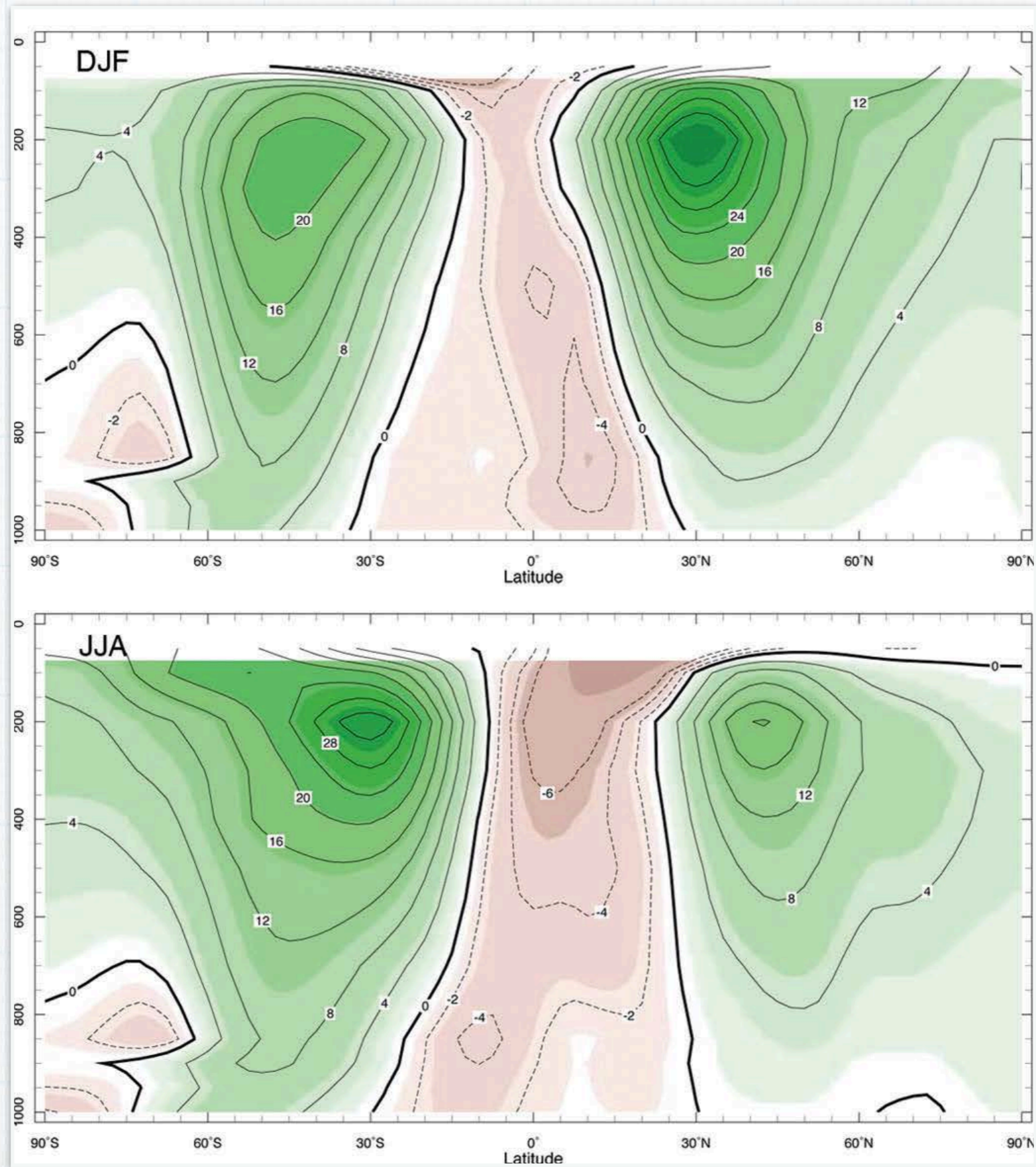
Wind

- There is a geopotential height slope from equator to pole
- We can expect that the pressure gradient force exists aloft.
- Wind has three dimensions: $\mathbf{u} = (u, v, w)$
↓
Hard to measure

Wind - zonal wind (u)



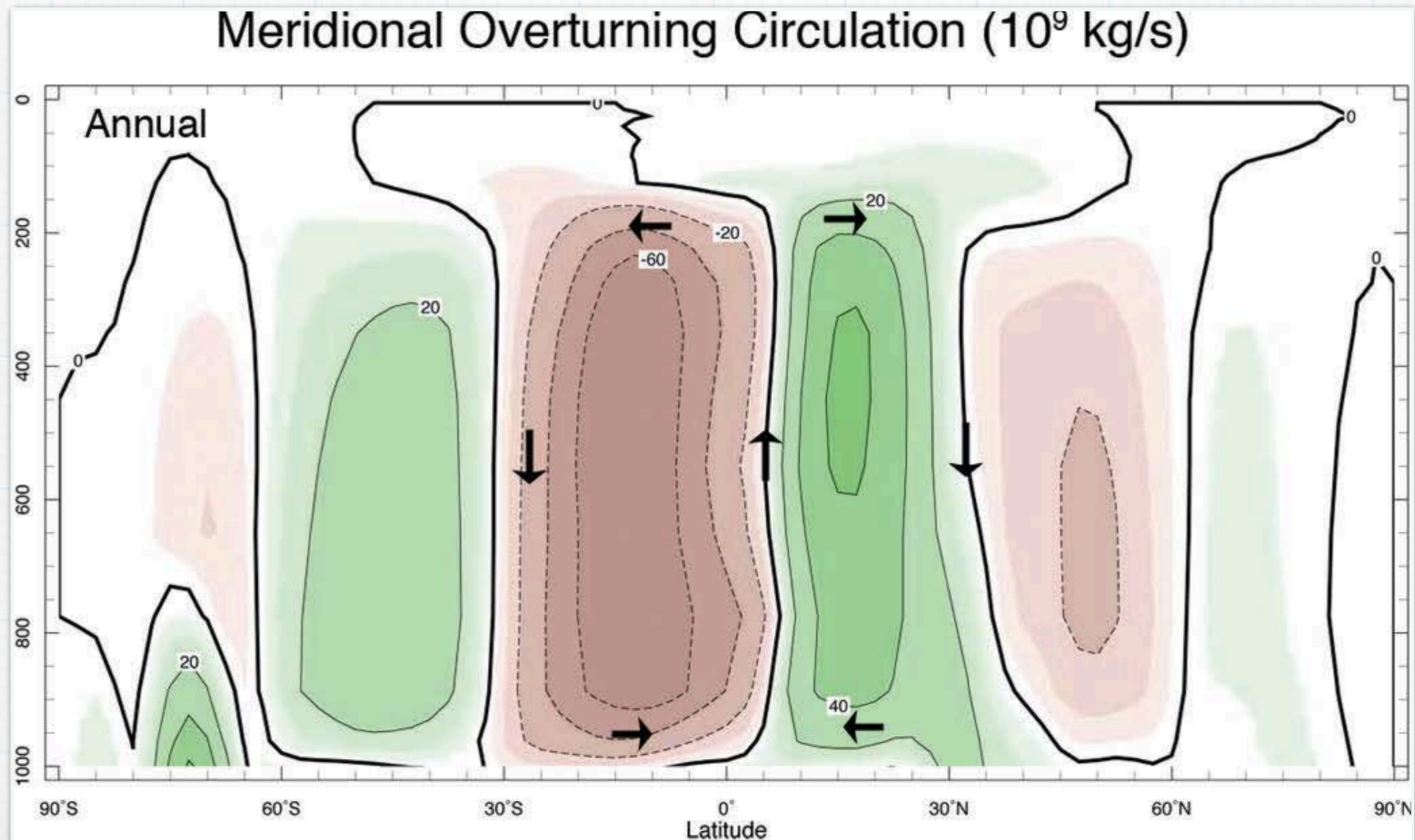
Wind - zonal wind (u)



Wind - meridional wind (v)

$$v = - \frac{1}{\rho a \cos \phi} \frac{\partial \Psi}{\partial z}$$

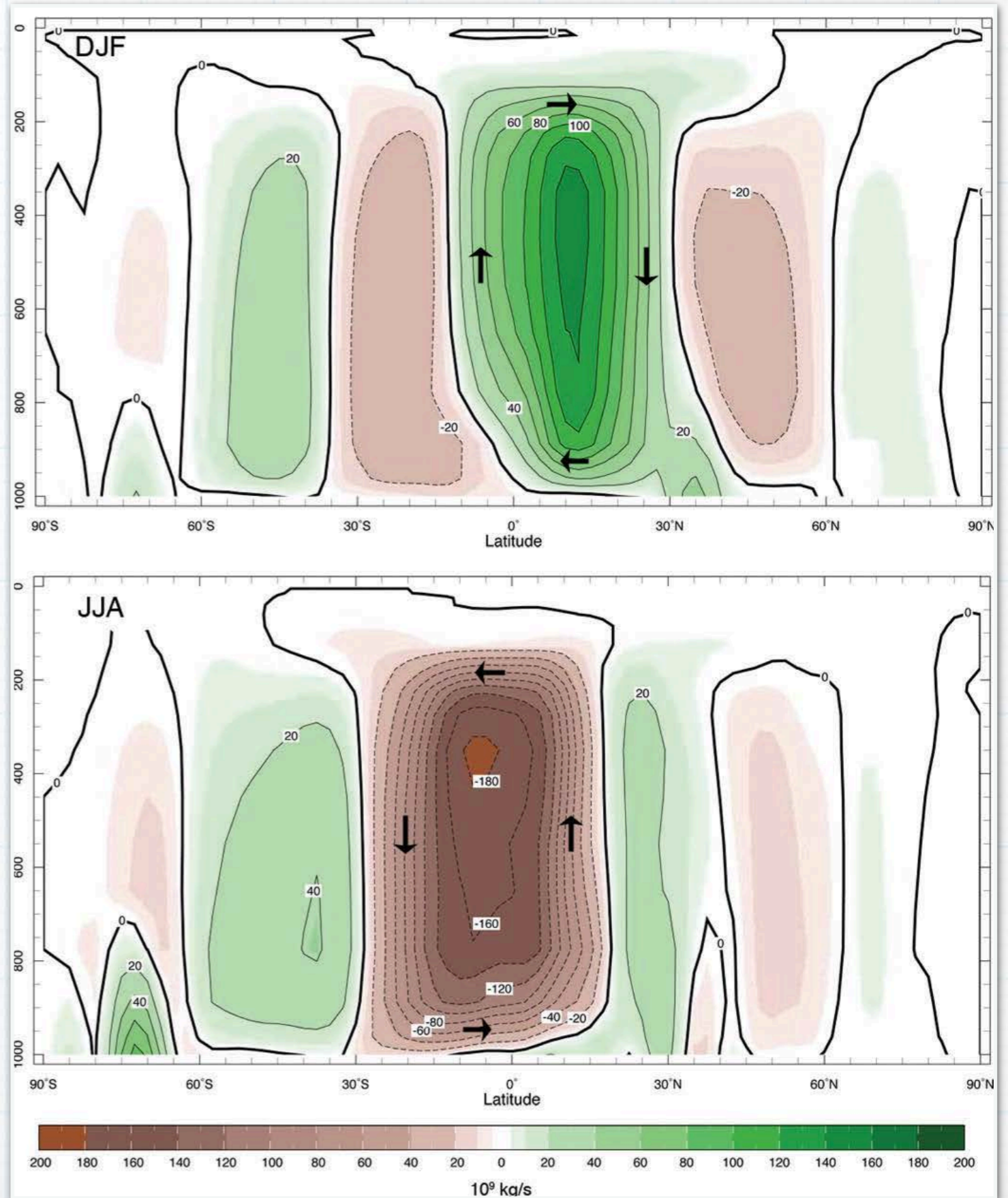
$$w = \frac{1}{\rho a^2 \cos \phi} \frac{\partial \Psi}{\partial \phi}$$



Wind - meridional wind (v)

$$v = - \frac{1}{\rho a \cos \phi} \frac{\partial \Psi}{\partial z}$$

$$w = \frac{1}{\rho a^2 \cos \phi} \frac{\partial \Psi}{\partial \phi}$$



Eddies and waves

